



## INDIAN SCHOOL AL WADI AL KABIR

ASSESSMENT II (2025 - 2026)

Answer Key

Class: XI

Sub: MATHEMATICS (041)

Max Marks: 80

Date:04.12.2025

Time:3 hour

1	(C) 4
2	(A) $(A \cup B)' = \{5, 7, 9\}$
3	(C) 1
4	(B) $x \in \mathbb{R} - \{3, -3\}$
5	(D) 0
6	(C) 13
7	(B) 0
8	(A) $x \in (-\infty, 120]$
9	(A) 9
10	(B) 3
11	(A) 110
12	(A) 300
13	(B) 26
14	(B) 80
15	(B) 11
16	(A) 1
17	(D) (-1, -1)
18	(C) -1
19	(d) Assertion (A) is false but reason (R) is true.
20	(c) Assertion (A) is true but reason (R) is false.

21	<p><math>A - B = \{2,3\}</math>  <math>C' = \{1,2,5,6,7\}</math></p> <p><math>((A - B) \cup C') = \{1,2,3,5,6,7\}</math></p>	<p>1 M  <math>\frac{1}{2}</math> M  <math>\frac{1}{2}</math> M</p>
22	<p>a</p> $\begin{aligned} \text{L.H.S.} &= \frac{\cos(\pi + x) \cos(-x)}{\sin(\pi - x) \cos\left(\frac{\pi}{2} + x\right)} \\ &= \frac{-\cos x \cos x}{-\sin x \sin x} \\ &= \cot^2 x \\ &= \text{R.H.S.} \end{aligned}$ <p style="text-align: center;">OR</p> <p>b</p> $\begin{aligned} \text{L.H.S.} &= \sin(n+1)x \sin(n+2)x + \cos(n+1)x \cos(n+2)x \\ &= \cos\{(n+1)x - (n+2)x\} \\ &= \cos(nx + x - n - 2x) \\ &= \cos(-x) \\ &= \cos(x) \end{aligned}$	<p>1 M  1 M  1 M  1 M</p>
23	<p>Step 1: Simplify numerator  <math>z_1 + z_2 + 1 = (2 - i) + (1 + i) + 1 = 4</math></p> <p>Step 2: Simplify denominator  <math>z_1 - z_2 + 1 = (2 - i) - (1 + i) + 1 = 2 - 2i</math></p> <p>Step 3: Divide and rationalize</p> $\frac{4}{2 - 2i} = \frac{4}{2(1 - i)} = \frac{2}{1 - i}$ $\frac{2}{1 - i} \cdot \frac{1 + i}{1 + i} = \frac{2(1 + i)}{2} = 1 + i$	<p><math>\frac{1}{2}</math> M  <math>\frac{1}{2}</math> M  <math>\frac{1}{2}</math> M  <math>\frac{1}{2}</math> M</p>
24	<p>Vowels: A, I, E (3) <math>\rightarrow</math> must occupy odd positions (1, 3, 5, 7)</p> <p>(i) Choose 3 odd positions for vowels: <math>{}^4C_3 = 4</math></p> <p>(ii) Arrange vowels: <math>3! = 6 \Rightarrow</math> Total vowel arrangements = <math>4 \times 6 = 24</math></p> <p>(iii) Arrange consonants (4 letters in remaining 4 positions): <math>4! = 24</math></p> <p>Total arrangements = <math>24 \times 24 = \boxed{576}</math></p>	<p>1 M  <math>\frac{1}{2}</math> M  <math>\frac{1}{2}</math> M</p>
25	<p>Ans: Let <math>r</math> be common ratio of the G.P. <math>a, b, c, d</math> then <math>b = ar, c = ar^2</math> and <math>d = ar^3</math>.</p> <p><math>\therefore a + b = a + ar = a(1 + r); b + c = ar + ar^2 = ar(1 + r); c + d = ar^2(r + 1)</math></p> <p>Now, <math>(b + c)^2 = [ar(1 + r)]^2 = [a(1 + r)][ar^2(1 + r)] = (a + b)(c + d)</math></p> <p><math>\therefore a + b, b + c, c + d</math> are in G. P.</p> <p style="text-align: center;">OR</p> $S_n = \frac{4}{9} \left( \sum_{k=1}^n 10^k - \sum_{k=1}^n 1 \right) = \frac{4}{9} \left( \frac{10(10^n - 1)}{9} - n \right)$ $\frac{4}{81} (10^{n+1} - 10 - 9n)$	<p>1 M  1 M  1 M  1 M</p>

26	(i) 140 (ii) 90 (iii) 20	1 M  1M  1M
27	(i) Domain (F) = [-2, 2] (ii) $\mathbb{R} - \{1,4\}$  OR  (i) $\mathbb{R} = \{(1,1), (1,2), (1,3), (1,4), (1,6), (2,4), (2,6), (3,6)\}$ (ii) Domain = {1,2,3},  Range = {1,2,3,4,6}	1.5 M 1.5 M   1 M 1M  1M
28	A is in Quadrant III (where sine is negative). B is in Quadrant IV (where sine is negative).  $\sin A = -\frac{7}{25}$  $\sin B = -\frac{4}{5}$  $\sin(A + B) = \left(\frac{-7}{25}\right)\left(\frac{3}{5}\right) + \left(\frac{-24}{25}\right)\left(\frac{-4}{5}\right)$  $= \frac{3}{5}$  OR  $\tan\left(\frac{\pi}{4} + x\right) = \frac{1 + \tan x}{1 - \tan x}$  $\tan\left(\frac{\pi}{4} - x\right) = \frac{1 - \tan x}{1 + \tan x}$  $= \frac{1 + \tan x}{1 - \tan x} \times \frac{1 + \tan x}{1 - \tan x} = \left(\frac{1 + \tan x}{1 - \tan x}\right)^2$	1 M  1 M  $\frac{1}{2}$ M  $\frac{1}{2}$ M    1 M  1 M  1 M
29	$7.2 \leq \frac{7.48 + 7.85 + x}{3} \leq 7.8$	1 M  1.5 M

	$7.2 \leq \frac{15.33 + x}{3} \leq 7.8$ $21.6 \leq 15.33 + x \leq 23.4$ $6.27 \leq x \leq 8.07$					$\frac{1}{2} M$																															
30	<table border="1"> <thead> <tr> <th><math>x_i</math></th> <th><math>f_i</math></th> <th>Cumulative Frequency</th> <th><math> x_i - M </math></th> <th><math>f_i x_i - M </math></th> </tr> </thead> <tbody> <tr> <td>10</td> <td>2</td> <td>2</td> <td>2</td> <td>4</td> </tr> <tr> <td>11</td> <td>3</td> <td>5</td> <td>1</td> <td>3</td> </tr> <tr> <td>12</td> <td>8</td> <td>13</td> <td>0</td> <td>0</td> </tr> <tr> <td>14</td> <td>3</td> <td>16</td> <td>2</td> <td>6</td> </tr> <tr> <td>15</td> <td>4</td> <td>20</td> <td>3</td> <td>12</td> </tr> <tr> <td></td> <td><math>\sum f_i = 20</math></td> <td></td> <td></td> <td><math>\sum f_i x_i - M  = 25</math></td> </tr> </tbody> </table>	$x_i$	$f_i$	Cumulative Frequency	$ x_i - M $	$f_i x_i - M $	10	2	2	2	4	11	3	5	1	3	12	8	13	0	0	14	3	16	2	6	15	4	20	3	12		$\sum f_i = 20$			$\sum f_i x_i - M  = 25$	1.5 M
$x_i$	$f_i$	Cumulative Frequency	$ x_i - M $	$f_i x_i - M $																																	
10	2	2	2	4																																	
11	3	5	1	3																																	
12	8	13	0	0																																	
14	3	16	2	6																																	
15	4	20	3	12																																	
	$\sum f_i = 20$			$\sum f_i x_i - M  = 25$																																	
	<p>Median=12</p> $MD = \frac{\sum f_i x_i - M }{N} = \frac{25}{20}$ <p>= 1.25</p>					$\frac{1}{2} M$																															
31	<p>Ans: <math>6^n - 5n - 1 = (1 + 5)^n - 5n - 1</math>  <math>= [1 + 5n + {}^nC_2 \cdot 5^2 + {}^nC_3 \cdot 5^3 + \dots 5^n] - 5n - 1</math>  <math>= 25[{}^nC_2 + 5 \cdot {}^nC_3 + \dots 5^{n-2}]</math>  which is divisible by 25.</p>					1 M 1 M 1 M																															
32	<p>(i) <math>11C_4 = 330</math>  (ii) <math>6C_2 \times 5C_2 = 150</math>  (iii) <math>6C_4 + 5C_4 = 20</math>  (iv) <math>5C_2 \times 6C_2 + 5C_3 \times 6C_1 + 5C_4 = 215</math></p>					1 M 1 M 1 M 2 M																															
33	$(\sqrt{2} + 1)^6 - (\sqrt{2} - 1)^6 = 2 \left[ \binom{6}{1}(\sqrt{2})^1 + \binom{6}{3}(\sqrt{2})^3 + \binom{6}{5}(\sqrt{2})^5 \right]$ $= 2 \left[ 6(\sqrt{2}) + 20(\sqrt{2})^3 + 6(\sqrt{2})^5 \right]$ $(\sqrt{2} + 1)^6 - (\sqrt{2} - 1)^6 = 140\sqrt{2}$ $140 \cdot 1.414 = 197.96$ $(\sqrt{2} + 1)^6 \text{ lies between } 197 \text{ and } 198$					1.5 M 1 M 1.5 M 1 M																															

34	<p>(i) Given <math>\frac{AM}{GM} = \frac{\frac{a+b}{2}}{\sqrt{ab}} = \frac{m}{n}</math>.</p> <p>Let <math>\frac{a+b}{2} = mk</math>, <math>\sqrt{ab} = nk</math>.</p> <p>Then <math>a + b = 2mk</math>, <math>ab = n^2k^2</math>.</p> <p>So <math>a</math> and <math>b</math> are roots of <math>x^2 - 2mkx + n^2k^2 = 0</math>.</p> <p>Roots: <math>x = k(m \pm \sqrt{m^2 - n^2})</math>.</p> <p>Hence, <math>a : b = (m + \sqrt{m^2 - n^2}) : (m - \sqrt{m^2 - n^2})</math>.</p> <p style="text-align: center;">OR</p> <p>The roots form a G.P.: <math>a, ar, ar^2, ar^3</math>.</p> <p>From <math>a + b = 3</math>,</p> $a + ar = 3 \Rightarrow a(1 + r) = 3$ <p>From <math>c + d = 12</math>,</p> $ar^2 + ar^3 = 12 \Rightarrow ar^2(1 + r) = 12 \Rightarrow 3r^2 = 12 \Rightarrow r^2 = 4 \Rightarrow r^4 = 16$ <p>Also,</p> $p = ab = a^2r, \quad q = cd = a^2r^5$ $\frac{q + p}{q - p} = \frac{r^5 + r}{r^5 - r} = \frac{r^4 + 1}{r^4 - 1} = \frac{16 + 1}{16 - 1} = \frac{17}{15}$ $\therefore (q + p) : (q - p) = 17 : 15$	<p>1 M</p> <p>1 M</p> <p>1 M</p> <p>1 M</p> <p>1 M</p> <p>1 M</p> <p>1.5 M</p> <p>1 M</p> <p>1.5 M</p>
35	<p>a</p> <p>Let the point of intersection of the two given lines be <math>P(x_1, y_1)</math>.</p> $2x - 3y + 4 = 0 \quad (1)$ $3x + 4y - 5 = 0 \quad (2)$ <p>Solving (1) and (2): <math>P(x_1, y_1) = \left(\frac{-1}{17}, \frac{22}{17}\right)</math></p> <p>The given line is <math>6x - 7y + 8 = 0</math>. Its slope is <math>m_1 = \frac{6}{7}</math>.</p> <p>Since the required path is perpendicular, its slope will be</p> $m_2 = -\frac{1}{m_1} = -\frac{7}{6}$ <p>Therefore, the equation of the line using one-point form,</p> $y - y_1 = m(x - x_1)$ $y - \left(\frac{22}{17}\right) = -\frac{7}{6}\left(x - \frac{-1}{17}\right)$ $119x + 102y = 125$ <p style="text-align: center;">OR</p> <p>Given point <math>P(1,2)</math> and mirror line <math>x - 3y + 4 = 0</math>. Let the image be <math>P'(x, y)</math>.</p> <p>(1) Midpoint lies on the mirror:</p> <p>Midpoint <math>M</math> of <math>PP'</math> is</p> $M\left(\frac{1+x}{2}, \frac{2+y}{2}\right).$ <p>Since <math>M</math> lies on <math>x - 3y + 4 = 0</math>,</p>	<p>1.5 M</p> <p>1 M</p> <p>1.5 M</p> <p>1 M</p> <p>1 M</p>
	<p>b</p>	

	$\frac{1+x}{2} - 3 \cdot \frac{2+y}{2} + 4 = 0 \Rightarrow x - 3y + 3 = 0$ <p>(2) <math>PP'</math> is perpendicular to the mirror:</p> <p>Slope of <math>x - 3y + 4 = 0</math> is <math>\frac{1}{3}</math>, hence slope of <math>PP'</math> is <math>-3</math>.</p> $\frac{y-2}{x-1} = -3 \Rightarrow 3x + y - 5 = 0$ <p>Solving (A) and (B):</p> $x = \frac{3}{5}, \quad y = -\frac{1}{5} \quad \therefore \text{Image of } (1,2) \text{ is } \left(\frac{6}{5}, \frac{7}{5}\right).$	1 M 1 M 1 M 1 M
36	<p>(i) Number of ways of selecting 3 questions from Section A and 4 from Section B:</p> ${}^5C_3 \times {}^7C_4 = \boxed{350}$ <p>(ii) Student answers at least 3 questions from each section. Possible selections are: (3 from A, 4 from B), (4 from A, 3 from B),</p> $\Rightarrow {}^5C_3 {}^7C_4 + {}^5C_4 {}^7C_3 = 10 \times 35 + 5 \times 35 = 350 + 175 = 525$ <p><math>\therefore</math> Total ways = <math>\boxed{525}</math></p>	1 M 1 M 1 M 1 M
37	<p>Given the GP for pots: <math>a = 2, r = 2</math>. Thus <math>t_n = 2^n</math> and</p> $S_n = a \frac{r^n - 1}{r - 1} = 2(2^n - 1) = 2^{n+1} - 2.$ <p>(i) Difference between 7th and 5th row:</p> $t_7 - t_5 = 2^7 - 2^5 = 128 - 32 = \boxed{96}.$ <p>(ii) Total pots in first ten rows:</p> $S_{10} = 2(2^{10} - 1) = 2(1024 - 1) = 2 \times 1023 = \boxed{2046}.$ <p>(iii a) If total pots = 510, find number of rows <math>n</math>:</p> $2^{n+1} - 2 = 510 \Rightarrow 2^{n+1} = 512 = 2^9 \Rightarrow n + 1 = 9 \Rightarrow \boxed{n = 8}.$ <p>OR</p> <p>(iii b) For <math>a = 1, r = 3</math> and total = 1093:</p> $\frac{3^n - 1}{2} = 1093 \Rightarrow 3^n - 1 = 2186 \Rightarrow 3^n = 2187 = 3^7 \Rightarrow \boxed{n = 7}.$	1 M 1 M 2 M 2 M
38	<p>i) <math>\frac{-1}{3}</math></p> <p>ii) <math>13x - y - 9 = 0</math></p> <p>iii) Slope = 3 <math>3x - y + 1 = 0</math></p> <p style="text-align: center;">(OR)</p> <p>(iii) Slope = 3 <math>3x - y - 4 = 0</math></p>	1 M 1 M 1 M 1 M 1 M 1 M

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